

ADVANCED TOPICS

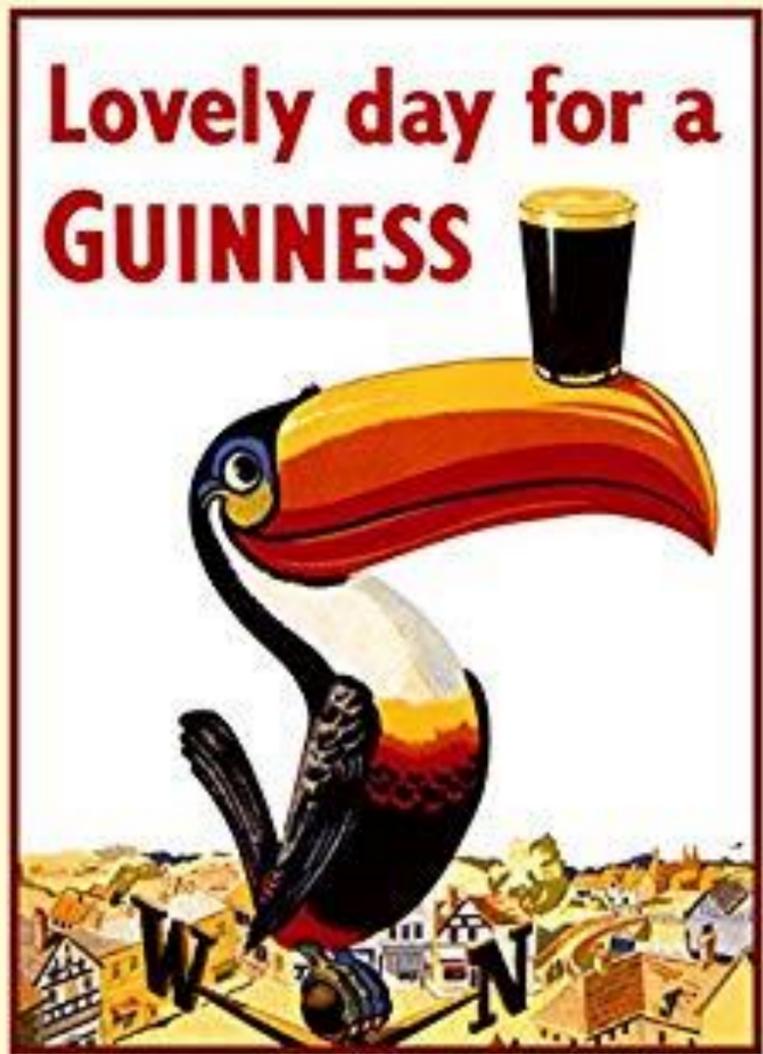
NEXT-LEVEL DIRECT MARKETING

Table 3. Number of experimental runs (n_{exp}), maximum number of factors (n_f), levels (L_i) and maximum number of factors for specified levels ($\sum MF_i$)

n_{exp}	n_f	L_1	$\sum MF_1$	L_2	$\sum MF_2$	L_3	$\sum MF_3$	n_{exp}	n_f	L_1	$\sum MF_1$	L_2	$\sum MF_2$	L_3	$\sum MF_3$
4	3	4	2	2	1			12	5	12	1	2	4		
		2	3							6	5				
6	3	6	1	3	2					4	2	3	2	2	1
		3	3							4	1	3	2	2	2
		2	1	3	2					3	1	2	4		
8	7	4	4	2	3				4	12	4				
		4	2	2	5				3	12	1	6	2		
		2	7					14	6	7	5	2	1		
	6	8	3	4	2	2	1		5	14	1	7	4		
		8	1	4	3	2	2	15	8	5	4	3	4		
		8	1	4	1	2	4		7	5	5	3	2		
		4	6							15	1	3	6		
	5	8	3	2	2					5	2	3	5		
		8	2	2	3					5	1	3	6		
		8	1	4	3	2	1			3	7				
		8	1	2	4				6	15	1	5	5		
	4	8	4							5	6				
9	5	3	5							5	3	3	3		
	4	9	4					16	15	2	15				
		9	2	3	2				14	4	1	2	13		
		9	1	3	3				13	8	1	2	12		
10	6	10	1	5	5					4	2	2	11		
	3	5	2	2	1				12	16	1	2	11		
12	11	2	11						10	16	1	8	1	2	8
	10	4	1	2	9				9	4	9				
	9	4	2	2	7					4	3	2	6		
	7	4	4	2	3				7	8	7				
		4	3	2	4				5	16	5				
		3	7							16	2	2	3		
	6	4	6												
		4	3	3	1	2	2								
		4	2	3	1	2	3								
		3	4	2	2										
		3	3	2	3										

n_{exp} = number of experimental runs
 n_f = total number of factors
 L_i = levels for associated number of factors i
 $\sum MF_i$ = total number of maximum factors i

“Design of Experiments: Useful Orthogonal Arrays for Number of Experiments from 4 to 16”. Sorana D. Bolboacă and Lorentz Jäntschi, Entropy 2009.





William S. Gosset

- “Student”
- More like the (brew) Master
- Hoppy to see you
- Significant Other
- Rules are made to be broken



R.A. Fisher

- I, 95
- Do ya think (my son is) sexy?
- The Lady and the Tea

Muriel Bristol

- That's no lady
- The most important issue of the day
- A lady with taste
- Trust but verify
- Socks would have been nice too

<https://rss.onlinelibrary.wiley.com/doi/full/10.1111/j.1740-9713.2012.00620.x>



R.A. Fisher

- Designing Experiments
- Not great, Ron
- A pun about Kolkata

Genichi Taguchi

- KimoNO
- Rao your boat
- OrthagonAlley
- You can drive my car
- Method Man



C.R. Rao

A/B Testing

Envelope
Color

Message



*DMAW is
Great!*

*DMAW is
Really Great!*

Test 1:



vs.



(which message?)

Test 2:

*DMAW is
Great!*

vs.

*DMAW is
Really Great!*

(which envelope color?)

Full Factorial Testing

Envelope
Color

Message



*DMAW is
Great!*

*DMAW is
Really Great!*

Test 1:



*DMAW is
Great!*

Test 2:



*DMAW is
Really Great!*

Test 3:



*DMAW is
Great!*

Test 4:



*DMAW is
Really Great!*

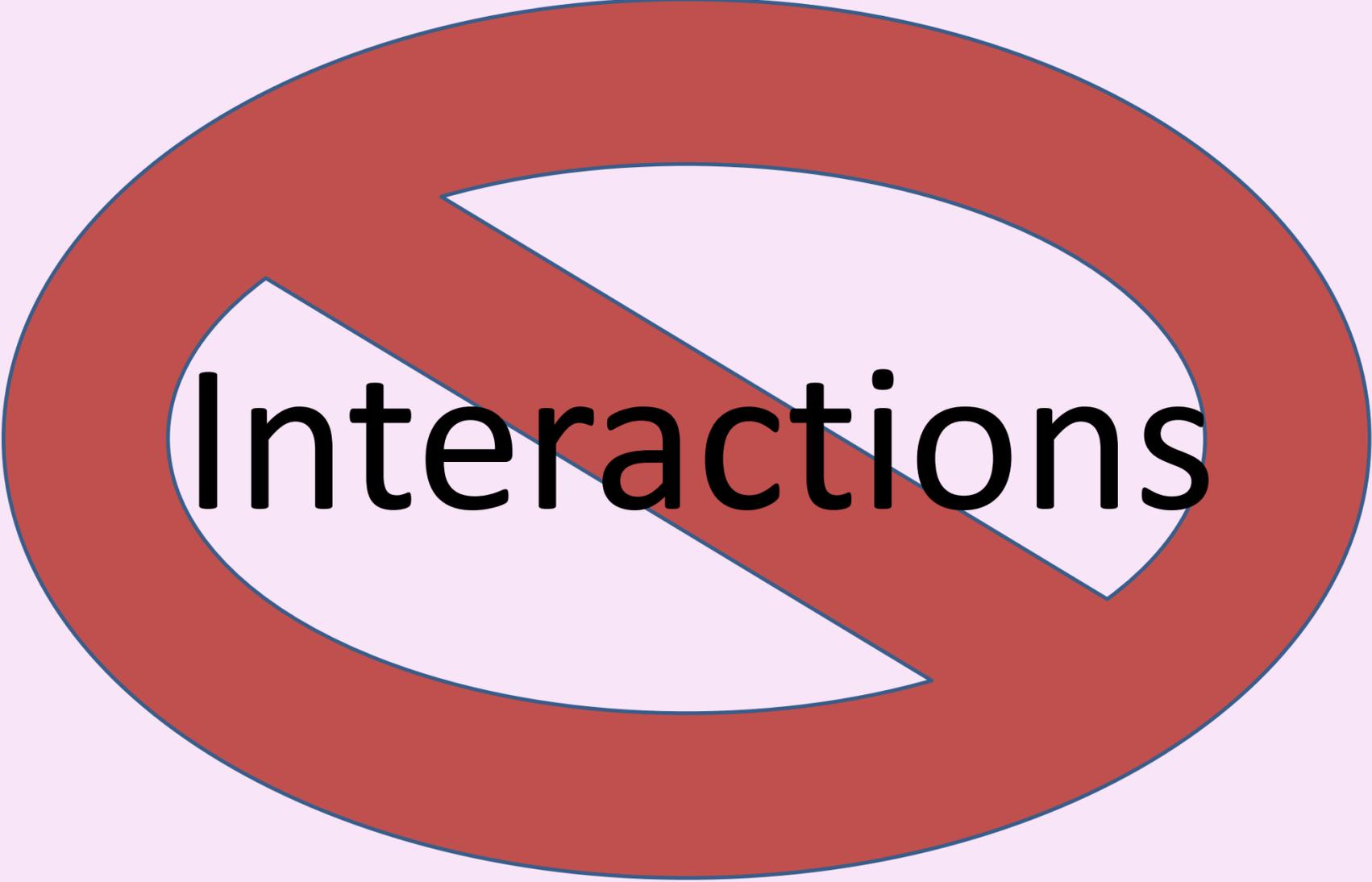
Terms to Know

Factor – The groups of things to be tested. (e.g. Envelope Color or Messaging)

Level – The different values within a factor. (e.g.: Red or Blue; DMAW is Great! or DMAW is Really Great!)

Qualitative/Quantitative – Describes the factors and levels we are testing. Most are qualitative (color, messaging, etc.) Continuous numeric values are quantitative

Interaction – Two or more factors having a multiplicative impact (e.g. pouring sugar AND stirring tea)



Interactions

Full Factorial Testing

Envelope
Color

Message



*DMAW is
Great!*

*DMAW is
Really Great!*

Test 1:



*DMAW is
Great!*

Test 2:



*DMAW is
Really Great!*

Test 3:



*DMAW is
Great!*

Test 4:



*DMAW is
Really Great!*

Full Factorial Testing

Envelope Color	Message	Envelope Color	Message
		Test 1:	1 1
 (1)	<i>DMAW is Great!</i> (1)	Test 2:	1 2
 (2)	<i>DMAW is Really Great!</i> (2)	Test 3:	2 1
		Test 4:	2 2

Full Factorial Testing

Envelope Color

Message

Font



(1)



(2)



(3)

DMAW is Great! (1)

DMAW is Really Great! (2)

Arial (1)

Times

New (2)

Roman

Test #	Envelope Color	Message	Font
1	1	1	1
2	1	1	2
3	1	2	1
4	1	2	2
5	2	1	1
6	2	1	2
7	2	2	1
8	2	2	2
9	3	1	1
10	3	1	2
11	3	2	1
12	3	2	2

Full Factorial Testing – Number of Tests Required

Envelope
Color: 3

Message:
2

Font:
2



(1)



(2)



(3)

*DMAW is
Great!* (1)

*DMAW is Really
Great!* (2)

Arial (1)

Times
New (2)
Roman

$$3 \times 2 \times 2 = 12$$

AARP Test from 2015

Envelope	Letter	Reply	RAE	Ask
Pre-Renewal Monarch OE	Pre-Renewal Letter	Pre-Renewal Reply	Pre-Renewal RAE	\$12
#10 OE	Double Reply Letter	Double Reply Faux NCR Format	3 ways to give on back of RAE	3 ask test
Brownkraft	Faux NCR Letter	Pre-Renewal Reply Redesign	Note pushing for online gift	\$12.50
Respond by Date	Remove BBB Logo	Double Reply Format		

4

4

4

3

3

Control

$$4 \times 4 \times 4 \times 3 \times 3 = ???$$

Fractional Factorial

Test #	Envelope	Letter	Reply	RAE	Ask
1	1	1	1	1	1
2	2	1	1	1	0
3	3	1	1	0	3
4	4	1	4	3	1
5	1	2	4	3	1
6	2	2	4	2	1
7	3	2	4	2	2
8	4	2	3	3	2
9	1	3	3	1	3
10	2	3	3	2	3
11	3	3	1	2	1
12	4	3	2	3	3
13	1	4	2	3	3
14	2	4	3	1	2
15	3	4	2	2	2
16	4	4	2	1	2

Full Factorial

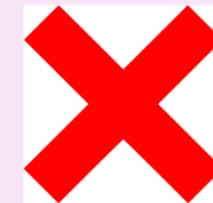
Fractional Factorial

Tests

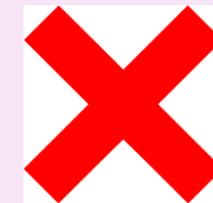
576

16

Measure
Interactions?



Test all
combinations?



Packages	Qty	Response	RR%	Income	Cost	Net/Donor
Pre-Ren Rem No Prem Offer #10 OE No BBB Ltr DR Rep 3 ways RAE MV Tst #4	30,000	428	1.43%	\$ 5,974.00	\$ 6,280.24	\$ (0.71)
Pre-Ren Rem No Prem Offer Faux NCR Ltr DR Rep Onl Push RAE MV Tst #2	30,000	399	1.33%	\$ 5,523.99	\$ 5,611.56	\$ (0.22)
Pre-Ren Rem No Prem Offer #10 OE Faux NCR Ltr DR NCR Rep 3 ways RAE 3 Ask MV Tst #15	30,000	366	1.22%	\$ 5,650.00	\$ 7,282.24	\$ (4.38)
Pre-Ren Rem No Prem Offer Resp by OE DR Rep 3 Ask MV Tst #12	30,000	366	1.22%	\$ 5,114.00	\$ 5,298.06	\$ (0.50)
Pre-Ren Rem No Prem Offer #10 OE DR Ltr MV Tst #1	30,000	354	1.18%	\$ 5,319.00	\$ 6,558.82	\$ (3.46)
Pre-Ren Rem No Prem Offer 3 ways RAE \$12.50 Ask MV Tst #10	30,000	353	1.18%	\$ 5,193.30	\$ 5,016.06	\$ 0.50
Pre-Ren Rem No Prem Offer Resp by OE DR Ltr DR NCR Rep 3 ways RAE \$12.50 Ask MV Tst #11	30,000	343	1.14%	\$ 5,008.00	\$ 11,283.65	\$ (18.19)
Pre-Ren Rem No Prem Offer DR Ltr DR NCR Rep 3 Ask MV Tst #13	30,000	334	1.11%	\$ 4,820.00	\$ 11,283.65	\$ (18.90)
Pre-Renewal Reminder w/ No BE Offer Ctrl	30,000	330	1.10%	\$ 4,649.00	\$ 5,016.06	\$ (1.09)
Pre-Ren Rem No Prem Offer Resp by OE Faux NCR Ltr Rep Redsgn 3 ways RAE MV Tst #5	30,000	310	1.03%	\$ 4,529.00	\$ 5,702.75	\$ (3.76)
Pre-Ren Rem No Prem Offer BK OE DR NCR Rep Onl Push RAE MV Tst #3	30,000	306	1.02%	\$ 4,336.00	\$ 7,411.08	\$ (9.95)
Pre-Ren Rem No Prem Offer BK DR Ltr DR Rep Onl Push \$12.50 Ask MV Tst #8	30,000	292	0.97%	\$ 4,111.50	\$ 6,229.67	\$ (7.23)
Pre-Ren Rem No Prem Offer BK OE Faux NCR Ltr \$12.50 Ask MV Tst #6	30,000	289	0.96%	\$ 4,321.50	\$ 6,169.08	\$ (6.33)
Pre-Ren Rem No Prem Offer No BBB Ltr Rep Redsgn \$12.50 Ask MV Tst #7	30,000	284	0.95%	\$ 4,067.00	\$ 5,016.06	\$ (3.31)
Pre-Ren Rem No Prem Offer #10 OE Rep Redsgn Onl Push RAE \$12.50 Ask MV Tst #9	30,000	270	0.90%	\$ 4,508.00	\$ 6,283.24	\$ (6.50)
Pre-Ren Rem No Prem Offer Resp by OE No BBB Ltr Onl Push RAE 3 Ask MV Tst #14	30,000	204	0.68%	\$ 3,586.00	\$ 5,016.06	\$ (6.88)
Pre-Ren Rem No Prem Offer BK OE DR Ltr Rep Redsgn 3 ways RAE 3 Ask MV Tst #16	30,000	127	0.42%	\$ 2,200.00	\$ 6,850.36	\$ (36.33)

Package	RAE		
	Pre-Renewal RAE	Note pushing for online gift	3 ways to give on back of RAE
1	1.18%		
2		1.33%	
3		1.02%	
4			1.43%
5			1.03%
6	0.96%		
7	0.95%		
8		0.97%	
9		0.90%	
10			1.18%
11			1.14%
12	1.22%		
13	1.11%		
14		0.68%	
15			1.22%
16			0.42%
control	1.10%		
Maximum	1.22%	1.33%	1.43%
Minimum	0.95%	0.68%	0.42%
Mean	1.09%	0.98%	1.07%
Rank	1	3	2

Step 1 – Isolate packages containing each element

Step 2 – Calculate mean response rate for each element

Step 3 – Determine “statistical significance” of best mean response rate to every other mean response rate

Step 4 – Analyze Maximum – Minimum (small difference suggests factor has big impact on response rate)

Step 5 – Analyze spread of mean response rates (big difference suggests big impact on response rate)

Winners and Retest

	Winner #1	Winner #2
Envelope	#10 OE	Pre-Renewal Monarch OE
Letter	Faux NCR Letter	Pre-Renewal Letter
Reply	Double Reply Format	
RAE	Pre-Renewal RAE	3 ways to give on back of RAE
Ask	\$12	

Winning package generated 26% lift in income, 18% lift in response, and cut Net/Sent and Net/Donor in half

Package	Envelope	Letter	Reply	RAE	Ask
1	#10 OE	Faux NCR Letter	Double Reply Format	Pre-Renewal RAE	\$12
2	#10 OE	Faux NCR Letter	Double Reply Format	3 ways to give on back of RAE	\$12
3	#10 OE	Pre-Renewal Letter	Double Reply Format	Pre-Renewal RAE	\$12
4	#10 OE	Pre-Renewal Letter	Double Reply Format	3 ways to give on back of RAE	\$12
5	Pre-Renewal Monarch OE	Faux NCR Letter	Double Reply Format	Pre-Renewal RAE	\$12
6	Pre-Renewal Monarch OE	Faux NCR Letter	Double Reply Format	3 ways to give on back of RAE	\$12
7	Pre-Renewal Monarch OE	Pre-Renewal Letter	Double Reply Format	Pre-Renewal RAE	\$12
8	Pre-Renewal Monarch OE	Pre-Renewal Letter	Double Reply Format	3 ways to give on back of RAE	\$12
Control	Pre-Renewal Monarch OE	Pre-Renewal Letter	Pre-Renewal Reply	Pre-Renewal RAE	\$12

Example Taguchi Designs

Run	X ₁	X ₂	X ₃	X ₄
1	1	1	1	1
2	1	2	2	2
3	1	3	3	3
4	2	1	2	3
5	2	2	3	1
6	2	3	1	2
7	3	1	3	2
8	3	2	1	3
9	3	3	2	1

Taguchi, $P=2, L=3$				Taguchi, $P=3, L=3$				
Run #	a	b	X	Run #	a	b	c	X
1	1	1	X ₁	1	1	1	1	X ₁
2	1	2	X ₂	2	1	2	2	X ₂
3	1	3	X ₃	3	1	3	3	X ₃
4	2	1	X ₄	4	2	1	2	X ₄
5	2	2	X ₅	5	2	2	3	X ₅
6	2	3	X ₆	6	2	3	1	X ₆
7	3	1	X ₇	7	3	1	3	X ₇
8	3	2	X ₈	8	3	2	1	X ₈
9	3	3	X ₉	9	3	3	2	X ₉

Experiment Number	Column						
	1	2	3	4	5	6	7
1	1	1	1	1	1	1	1
2	1	1	1	2	2	2	2
3	1	2	2	1	1	2	2
4	1	2	2	2	2	1	1
5	2	1	2	1	2	1	2
6	2	1	2	2	1	2	1
7	2	2	1	1	2	2	1
8	2	2	1	2	1	1	2

When to Use Fractional Factorial Tests

- Have the test quantity/package availability to support it
- Want to test a lot of different things
- Don't care about interactions
- Have someone who can design/evaluate responsibly